

# Math 115

## Spring 2017

### Lecture 20

Factor Completely:

$$\textcircled{1} 24x^3 - 16x^2$$

$$= 8x^2(3x - 2)$$

$$\textcircled{3} 3x(3x+2) + 2(3x+2)$$

$$= (3x+2)(3x+2)$$

$$= (3x+2)^2$$

$$\textcircled{2} 4x^3 - 5x^2 + 8x - 10$$

$$= x^2(4x-5) + 2(4x-5)$$

$$= (4x-5)(x^2+2)$$

$$\textcircled{4} x^2 - 7x - 30$$

$$= x^2 + 3x - 10x - 30$$

$$= x(x+3) - 10(x+3)$$

$$= (x+3)(x-10)$$

$P = -30$   
 $S = -7$   
 $3 \times -10$

⑤  $3x^2 - x - 10$   
 $P = -30$   
 $S = -1$   
 $5 \times -6 = -30$   
 $= 3x^2 + 5x - 6x - 10$   
 $= x(3x+5) - 2(3x+5)$   
 $= (3x+5)(x-2)$

⑥  $x^2 - 49$   
 $A^2 - B^2 = (A+B)(A-B)$   
 $= x^2 - 7^2$   
 $= (x+7)(x-7)$

⑦  $x^3 - 36x$   
 $= x(x^2 - 36)$   
 $= x(x+6)(x-6)$   
 $x^2 - 36 = x^2 - 6^2$

⑧  $x^2 + 12x + 36$   
 $= (x+6)^2$   
 $2(x)(6) = 12x$

⑨  $x^2 + 100$   
 $= x^2 + 10^2$  Prime  
 $A^2 + B^2$  is prime

⑩  $x^2 - 20x + 100$   
 $= (x-10)^2$   
 $2(x)(10)$

⑪  $4x^2 + 20x + 25$   
 $= (2x+5)^2$   
 $2(2x)(5)$

⑫  $x^3 + 64$   
 $x^3 + 4^3$   
 Use  $A^3 + B^3$   
 $= (A+B)(A^2 - AB + B^2)$   
 $= x^3 + 4^3$   
 $= (x+4)(x^2 - 4x + 16)$

$$\textcircled{13} \quad x^3 - 1000$$

$$= x^3 - 10^3$$

$$A^3 - B^3$$

$$= (x - 10)(x^2 + 10x + 100)$$

$$\textcircled{15} \quad x^3 + 3x^2 - 4x - 12$$

$$= x^2(x + 3) - 4(x + 3)$$

$$= (x + 3)(x^2 - 4)$$

$$= (x + 3)(x + 2)(x - 2)$$

$$\textcircled{14} \quad x^4 - 25x^2 \quad x^2 - 5^2$$

$$= x^2(x^2 - 25)$$

$$= x^2(x + 5)(x - 5)$$

$$\textcircled{16} \quad x^2 + 3x - 12$$

$$P = -12, S = 3$$

$$-1, 12$$

$$-2, 6$$

$$-3, 4$$

No Such numbers

Prime

$$\textcircled{17} \quad 4x^2 + 12x - 7$$

$$P = -28$$

$$-1, 28$$

$$-2, 14$$

$$-4, 7$$

$$S = 12$$

$$= 4x^2 - 2x + 14x - 7$$

$$= 2x(2x - 1) + 7(2x - 1)$$

$$= (2x - 1)(2x + 7)$$

$$\textcircled{18} \quad 125x^3 + 27$$

$$= (5x)^3 + (3)^3$$

$$= (5x + 3)(25x^2 - 15x + 9)$$

$$\textcircled{19} \quad 27x^3 - 125y^3$$

$$= (3x)^3 - (5y)^3$$

$$= (3x - 5y)(9x^2 + 15xy + 25y^2)$$

$$\textcircled{20} \quad 49x^2 - 70xy + 25y^2$$

$$(7x - 5y)^2$$

$$2(7x)(5y)$$

## Review ch. 4

1) Divide:  $\frac{48x^5 - 6x^3}{-3x^4}$

$$= \frac{48x^5}{-3x^4} - \frac{6x^3}{-3x^4}$$

$$= -16x + \frac{2}{x}$$

2) Divide:  $\frac{x^4 - 3x^3 + 5x - 7}{x - 2}$

$$\begin{array}{r}
 x-2 \overline{) x^4 - 3x^3 + 0x^2 + 5x - 7} \\
 \underline{x^3 - x^2 - 2x + 1} \phantom{0} \\
 -x^3 + 0x^2 + 5x - 7 \\
 \underline{-(-x^3 + 2x^2)} \phantom{0} \\
 -2x^2 + 5x - 7 \\
 \underline{-(-2x^2 + 4x)} \phantom{0} \\
 x - 7 \\
 \underline{-(x-2)} \\
 -5
 \end{array}$$

$$x \boxed{x^3} = x^4 - (x^4 - 2x^3)$$

$$x \boxed{-x^2} = -x^3 - (-x^3 + 2x^2)$$

$$x \boxed{-2x} = -2x^2 - (-2x^2 + 4x)$$

$$x \boxed{1} = x - (x - 2)$$

$$x^3 - x^2 - 2x + 1 + \frac{-5}{x-2}$$

## Class Quiz

Divide:

①  $\frac{45x^8 - 15x^2}{-3x^5}$

$$= \frac{45x^8}{-3x^5} - \frac{15x^2}{-3x^5}$$

$$= -15x^3 + \frac{5}{x^3}$$



②  $\frac{x^3 + 2x^2 - 5x + 2}{x - 1}$

$$\begin{array}{r}
 x-1 \overline{) x^3 + 2x^2 - 5x + 2} \\
 \underline{x^2 + 3x - 2} \phantom{0} \\
 x^3 + 2x^2 - 5x + 2 \\
 \underline{-(x^3 - x^2)} \phantom{0} \\
 3x^2 - 5x + 2 \\
 \underline{-(3x^2 - 3x)} \phantom{0} \\
 -2x + 2 \\
 \underline{-(-2x + 2)} \\
 0
 \end{array}$$

$$x \boxed{x^2} = x^3 - (x^3 - x^2)$$

$$x \boxed{3x} = 3x^2 - (3x^2 - 3x)$$

$$x \boxed{-2} = -2x - (-2x + 2)$$

Zero - Factor Rule (Maybe both)

Solve  $(x-3)(x+7)=0$

by Z.F.R.

$$x-3=0 \quad \text{or} \quad x+7=0$$

$$\boxed{x=3} \quad \text{or} \quad \boxed{x=-7}$$

$$\{-7, 3\}$$

Solve  $\underbrace{(2x-5)(3x+8)(x-10)}_{\text{Are Factored}} = \underbrace{0}_{\text{Zero}}$

by Z.F.R.

$$2x-5=0 \quad \text{or} \quad 3x+8=0 \quad \text{or} \quad x-10=0$$

$$2x = 5$$

$$x = 5/2$$

$$3x = -8$$

$$x = -\frac{8}{3}$$

$$x=10$$

$$\left\{-\frac{8}{3}, \frac{5}{2}, 10\right\}$$

Solve

$$3x(x+12)(2x-3)=0$$

one side is completely factored

Zero

By Z.F.R.

$$3x=0 \text{ or } x+12=0 \text{ or } 2x-3=0$$

$$x=\frac{0}{3}$$

$$x=0$$

$$x=-12$$

$$2x=3$$

$$x=\frac{3}{2}$$

$$\{-12, 0, \frac{3}{2}\}$$

Solve

$$x^2 - 36 = 0$$

Factor this side completely

$$x^2 - 6^2$$

$$A^2 - B^2$$

$$(x+6)(x-6)=0$$

By Z.F.R.

$$x+6=0$$

$$x=-6$$

$$x-6=0$$

$$x=6$$

$$\{\pm 6\}$$

Solve  $x^2 - 10 = 3x$

① Make one side = 0, and factor the other side.

$$x^2 - 10 - 3x = 0$$

$$x^2 - 3x - 10 = 0$$

$$(x - 5)(x + 2) = 0$$

② use Z.F.R. & Solve

$$x - 5 = 0 \quad \text{or} \quad x + 2 = 0$$

$$\boxed{x = 5}$$

$$\text{or} \quad \boxed{x = -2}$$

③ Ans. in Soln. Set

$$\boxed{\{-2, 5\}}$$

Solve  $9x^2 + 7x = 2$

① Make one side = 0, and factor the other side completely.

$$9x^2 \quad \boxed{+7x} \quad -2 = 0$$

-18

$$P = -18$$

$$S = 7$$

$$-1, 18$$

$$\boxed{-2, 9}$$

$$-3, 6$$

$$\left\{-1, \frac{2}{9}\right\}$$

$$9x^2 \quad \boxed{-2x + 9x} \quad -2 = 0$$

$$x(9x - 2) + 1(9x - 2) = 0$$

$$(9x - 2)(x + 1) = 0$$

by Z.F.R.

$$9x - 2 = 0 \quad \text{or} \quad x + 1 = 0$$

$$\vdots$$

$$x = \frac{2}{9}$$

$$\vdots$$

$$x = -1$$

Solve

$$3x^2 + 8x - 11 = 13 - 6x$$

① Make one side zero, and simplify the other side.

$$3x^2 + 8x - 11 - 13 + 6x = 0$$

$$3x^2 + 14x - 24 = 0$$

② Factor completely the non zero side.

$$3x^2 \boxed{+14x} - 24 = 3x^2 \boxed{-4x + 18x} - 24$$

$$P = -72$$

$$-1, 72$$

$$-2, 36$$

$$-3, 24$$

$$\boxed{-4, 18}$$

$$-6, 12$$

$$-8, 9$$

$$S = 14$$

$$= x(3x - 4) + 6(3x - 4)$$

$$= (3x - 4)(x + 6)$$

③ use Z.F.P.

$$(3x - 4)(x + 6) = 0$$

by Z.F.P.

$$3x - 4 = 0 \quad \text{or} \quad x + 6 = 0$$

$$\boxed{x = \frac{4}{3}}$$

$$\boxed{x = -6}$$

$$\Rightarrow \left\{ -6, \frac{4}{3} \right\}$$

find  $x$ 

$$x \text{ 5ft} \quad A = 30 \text{ ft}^2$$

$$x + 1 \text{ 6ft}$$

$$A = LW$$

$$x(x + 1) = 30$$

$$x^2 + x = 30$$

$$x^2 + x - 30 = 0$$

$$(x - 5)(x + 6) = 0$$

by Z.F.T.

$$\boxed{x = 5}, \quad \cancel{x = -6}$$



find L &amp; W

$$x \begin{array}{|l} \text{3ft} \\ \text{10ft} \end{array} A = 30 \text{ ft}^2$$

$$3x+1$$

-1, 90

-2, 45

-3, 30

-5, 18

-6, 15

$$\boxed{-9, 10}$$

3ft and 10ft

$$A = LW$$

$$x(3x+1) = 30$$

$$3x^2 + x = 30$$

$$3x^2 + x - 30 = 0$$

$$P = -90$$

$$S = 1$$

$$3x^2 - 9x + 10x - 30 = 0$$

$$3x(x-3) + 10(x-3) = 0$$

$$(x-3)(3x+10) = 0$$

(By Z.F.T.)

$$\boxed{x=3} \quad x = -10/3$$